## Mathematics test

## Paper 2 Calculator allowed

## TIER

Please read this page, but do not open the booklet until your teacher tells you to start. Write your name and the name of your school in the spaces below. If you have been given a pupil number, write that also.

> First name
$\qquad$
Last name $\qquad$
School

## Pupil number

$\square$

## Remember

- The test is 1 hour long.
- You may use a calculator in this test.
- You will need: pen, pencil, rubber, ruler, an angle measurer or protractor and a calculator.
- Some formulae you might need are on page 2.
- This test starts with easier questions.
- Try to answer all the questions.
- Write all your answers and working on the test paper do not use any rough paper.
- Check your work carefully.
- Ask your teacher if you are not sure what to do.

| For marker's | Total marks |  |
| :--- | :--- | :--- |
| use only | Borderline check |  |
|  |  |  |

## Instructions

## Answers

This means write down your answer or show your working and write down your answer.

## Calculators

You may use a calculator to answer any question in this test.

## Formulae

You might need to use these formulae.

Trapezium


$$
\text { Area }=\frac{(a+b)}{2} \times h
$$

## Prism



Volume $=$ area of cross-section $\times$ length

1. Look at this number chain.

14
(a) Fill in the missing numbers in the circles below.

$\times 13.5$


1 mark


1 mark
(b) Fill in the missing numbers in the arrows below.


2. Alika has a box of square tiles.

The tiles are three different sizes.


1 by 1 tile



3 by 3 tile

She also has a mat that is 6 cm by 6 cm .
36 of the 1 by 1 tiles will cover the mat.

(a) How many of the $\mathbf{2}$ by $\mathbf{2}$ tiles will cover the mat?


1 mark
(b) How many of the $\mathbf{3}$ by $\mathbf{3}$ tiles will cover the mat?
(c) Alika glues three tiles on her mat like this:


Complete the gaps below.

She could cover the rest of the mat by using another two 3 by 3 tiles, and another 1 by 1 tiles.

She could cover the rest of the mat by using another two 2 by 2 tiles, and another

1 by 1 tiles.
3. Some pupils are planning a disco.

They use the spreadsheet on the opposite page to work out their costs.

Use the spreadsheet to answer these questions.
(a) How much does each ticket cost?
$\square$ 1 mark
(b) Explain why column $\mathbf{C}$ always shows the same amount.
(c) The pupils will lose money if they do not sell many tickets.

The pupils want to make a profit.
What is the smallest number of tickets they need to sell?

(d) The pupils decide they want to make a profit of at least $\mathbf{£} \mathbf{2 0}$ Now what is the smallest number of tickets they need to sell?
(e) At the disco they sell 30 tickets.

Work out how much profit they make.
$\square$

| A | B | C | D | E | F |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> tickets we <br> might sell | Income <br> from selling <br> tickets | Hire of <br> hall | Cost of <br> food | Total <br> costs | Profit <br> or loss |


| 10 | $£ 40.00$ | $£ 46.50$ | $£ 15.00$ | $£ 61.50$ | $-£ 21.50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | $£ 44.00$ | $£ 46.50$ | $£ 16.50$ | $£ 63.00$ | $-£ 19.00$ |
| 12 | $£ 48.00$ | $£ 46.50$ | $£ 18.00$ | $£ 64.50$ | $-£ 16.50$ |
| 13 | $£ 52.00$ | $£ 46.50$ | $£ 19.50$ | $£ 66.00$ | $-£ 14.00$ |
| 14 | $£ 56.00$ | $£ 46.50$ | $£ 21.00$ | $£ 67.50$ | $-£ 11.50$ |
| 15 | $£ 60.00$ | $£ 46.50$ | $£ 22.50$ | $£ 69.00$ | $-£ 9.00$ |
| 16 | $£ 64.00$ | $£ 46.50$ | $£ 24.00$ | $£ 70.50$ | $-£ 6.50$ |
| 17 | $£ 68.00$ | $£ 46.50$ | $£ 25.50$ | $£ 72.00$ | $-£ 4.00$ |
| 18 | $£ 72.00$ | $£ 46.50$ | $£ 27.00$ | $£ 73.50$ | $-£ 1.50$ |
| 19 | $£ 76.00$ | $£ 46.50$ | $£ 28.50$ | $£ 75.00$ | $£ 1.00$ |
| 20 | $£ 80.00$ | $£ 46.50$ | $£ 30.00$ | $£ 76.50$ | $£ 3.50$ |
| 21 | $£ 84.00$ | $£ 46.50$ | $£ 31.50$ | $£ 78.00$ | $£ 6.00$ |
| 22 | $£ 88.00$ | $£ 46.50$ | $£ 33.00$ | $£ 79.50$ | $£ 8.50$ |
| 23 | $£ 92.00$ | $£ 46.50$ | $£ 34.50$ | $£ 81.00$ | $£ 11.00$ |
| 24 | $£ 96.00$ | $£ 46.50$ | $£ 36.00$ | $£ 82.50$ | $£ 13.50$ |
| 25 | $£ 100.00$ | $£ 46.50$ | $£ 37.50$ | $£ 84.00$ | $£ 16.00$ |
| 26 | $£ 104.00$ | $£ 46.50$ | $£ 39.00$ | $£ 85.50$ | $£ 18.50$ |
| 27 | $£ 108.00$ | $£ 46.50$ | $£ 40.50$ | $£ 87.00$ | $£ 21.00$ |
| 28 | $£ 112.00$ | $£ 46.50$ | $£ 42.00$ | $£ 88.50$ | $£ 23.50$ |
| 29 | $£ 116.00$ | $£ 46.50$ | $£ 43.50$ | $£ 90.00$ | $£ 26.00$ |

4. A cookery book shows how long, in minutes, it takes to cook a joint of meat.

| $\Delta$ Microwave oven |
| :---: |
| Time $=(12 \times$ weight in pounds $)+15$ |

## Electric oven

Time $=(30 \times$ weight in pounds $)+35$
(a) How long will it take to cook a 3 pound joint of meat in a microwave oven? minutes
(b) How long will it take to cook a 7 pound joint of meat in an electric oven?
minutes
(c) How much quicker is it to cook a 2 pound joint of meat in a microwave oven than in an electric oven?

Show your working.
minutes
5. (a) I have a square piece of card.

I cut along the dashed line to make two pieces of card.


Do the two pieces of card have the same area? Tick $(\checkmark)$ Yes or No.
$\geqslant$

No $\square$

Explain your answer.
(b) The card is shaded grey on the front, and black on the back.

I turn piece A over to see its black side.

Which of the shapes below shows the black side of piece A?


Put a tick $(\checkmark)$ under the correct answer.

6. (a) Tick $(\sqrt{ })$ any rectangles below that have an area of $12 \mathrm{~cm}^{2}$

(b) A square has an area of $100 \mathrm{~cm}^{2}$

What is its perimeter?
Show your working.
7. Here is a plan of a ferry crossing.

(a) Complete the accurate scale drawing of the ferry crossing below.

(b) What is the length of the ferry crossing on your diagram?

(c) The scale is $\mathbf{1} \mathbf{~ c m}$ to $\mathbf{2 0} \mathbf{m}$. Work out the length of the real ferry crossing. Show your working, and write the units with your answer.
$\square$
8. (a) You pay $\mathbf{£ 2 . 4 0}$ each time you go swimming.

Complete the table.

| Number of swims | 0 | 10 | 20 | 30 |
| ---: | :---: | :---: | :---: | :---: |
| Total cost (£) | 0 | 24 |  |  |

(c) A different way of paying is to pay a yearly fee of $\mathbf{£ 2 2}$

Complete the table.

| Number of swims | 0 | 10 | 20 | 30 |
| ---: | :---: | :---: | :---: | :---: |
| Total cost (£) | 22 | 36 |  |  |

(d) Now show this information on the same graph.

Join these points with a straight line.
(e) For how many swims does the graph show that the cost is the same for both ways of paying?

9. A teacher has $\mathbf{5}$ full packets of mints and $\mathbf{6}$ single mints.

The number of mints inside each packet is the same.


The teacher tells the class:
'Write an expression to show how many mints there are altogether. Call the number of mints inside each packet $y^{\prime}$

Here are some of the expressions that the pupils write:

(a) Write down two expressions that are correct.
$\qquad$
(b) A pupil says: 'I think the teacher has a total of 56 mints'.

Could the pupil be correct? Tick $(\checkmark)$ Yes or No.


Explain how you know.
10. A drink from a machine costs 55p


The table shows the coins that were put into the machine one day.

| Coins | Number of coins |
| :---: | :---: |
| $50 p$ | 31 |
| $20 p$ | 22 |
| $10 p$ | 41 |
| $5 p$ | 59 |

How many cans of drink were sold that day?
Show your working.
11. You can work out the cost of an advert in a newspaper by using this formula:
$C=15 n+75$
C is the cost in pounds
$\boldsymbol{n}$ is the number of words in the advert
(a) An advert has 18 words.

Work out the cost of the advert.
Show your working.

## £

(b) The cost of an advert is $\mathbf{£ 6 1 5}$

How many words are in the advert?
Show your working.
words
12. (a) A coach travels $\mathbf{3 0 0}$ miles at an average speed of $\mathbf{4 0} \mathbf{~ m p h}$.

For how many hours does the coach travel?
© ...... hours
1 mark
(b) An aeroplane flies $\mathbf{1 8 6 0}$ miles in $\mathbf{4}$ hours.

What is its average speed?

(c) A bus travels for $\mathbf{2} \frac{\mathbf{1}}{2}$ hours at an average speed of $\mathbf{2 4} \mathbf{~ m p h}$.

How far does the bus travel?
miles
13. A trundle wheel is used to measure distances.

Imran makes a trundle wheel, of diameter 50 cm .

(a) Calculate the circumference of Imran's trundle wheel.

Show your working.
cm
(b) Imran uses his trundle wheel to measure the length of the school car park.

His trundle wheel rotates 87 times.

What is the length of the car park, to the nearest metre?

m
14. Join pairs of algebraic expressions that have the same value when $\boldsymbol{a}=\mathbf{3}, \boldsymbol{b}=\mathbf{2}$ and $\boldsymbol{c}=\mathbf{6}$

One pair is joined for you.

15. A teacher asked two different classes:
'What type of book is your favourite?'
(a) Results from class $A$ (total 20 pupils):

| Type of book | Frequency |
| :---: | :---: |
| Crime | 3 |
| Non-fiction | 13 |
| Fantasy | 4 |

Complete the pie chart to show this information.
Show your working and draw your angles accurately.

## Class A


(b) The pie chart below shows the results from all of class $B$.

Each pupil had only one vote.

## Class B



The sector for Non-fiction represents 11 pupils.
How many pupils are in class $B$ ?
Show your working.
pupils
16. The label on a pot of yoghurt shows this information.

How many grams of protein does $\mathbf{1 0 0} \mathbf{g}$ of yoghurt provide?

Show your working.

| Yoghurt | $\mathbf{1 2 5} \mathbf{g}$ |
| :--- | ---: |
| Each 125 g provides |  |
| Energy | 430 kJ |
| Protein | 4.5 g |
| Carbohydrate | 11.1 g |
| Fat | 4.5 g |

17. (a) On the $\mathrm{cm}^{2}$ grid below, draw a right-angled triangle with an area of $\mathbf{1 2} \mathbf{c m}^{2}$ Use line $A B$ as one side of the triangle.

(b) Now draw an isosceles triangle with an area of $12 \mathbf{c m}^{2}$ Use line $A B$ as one side of the triangle.

